

Quiz #2 - Monday, September 12, 2005

Given the following NFA, answer questions 1-4.



$$Q = \{q_1, q_2, q_3\}$$

$$\Sigma = \{0, 1\}$$

$$q_0 = q_1$$

$$F = \{q_3\}$$

1. Give the formal definition of the NFA.

$$N = (Q, \Sigma, \sigma, q_0, F)$$

σ	0	1	ϵ
q_1	$\{q_2\}$	$\emptyset$	$\{q_2\}$
q_2	$\emptyset$	$\{q_3\}$	$\emptyset$
q_3	$\emptyset$	$\emptyset$	$\emptyset$

2. What language does the NFA recognize?

$$L(N) = \{w \mid w \text{ is } 1 \text{ or } 01\}$$

3. Give the regular expression which describes the language of the NFA.

$$1 \cup 01$$

$$\text{or } (0 \cup \epsilon)1$$

4. Convert the NFA into a DFA.

$$\text{DFA } M = (Q', \Sigma, \sigma', q_0', F')$$

$$Q' = \{\{q_1\}, \{q_2\}, \{q_3\}, \{q_1, q_2\}, \{q_1, q_3\}, \{q_2, q_3\}, \{q_1, q_2, q_3\}, \emptyset\}$$

$$\Sigma = \{0, 1\} \quad q_0' = \{q_1, q_2\} \quad F' = \{\{q_3\}, \{q_1, q_3\}, \{q_2, q_3\}, \{q_1, q_2, q_3\}\}$$

σ'	0	1
$\emptyset$	$\emptyset$	$\emptyset$
$\{q_1\}$	$\{q_2\}$	$\emptyset$
$\{q_2\}$	$\emptyset$	$\{q_3\}$
$\{q_3\}$	$\emptyset$	$\emptyset$
$\{q_1, q_2\}$	$\{q_2\}$	$\{q_3\}$
$\{q_1, q_3\}$	$\{q_2\}$	$\emptyset$
$\{q_2, q_3\}$	$\emptyset$	$\{q_3\}$
$\{q_1, q_2, q_3\}$	$\{q_2\}$	$\{q_3\}$

